Diagram for Allen Fractal Closure Law (AFCL) in Pattern Field Theory™

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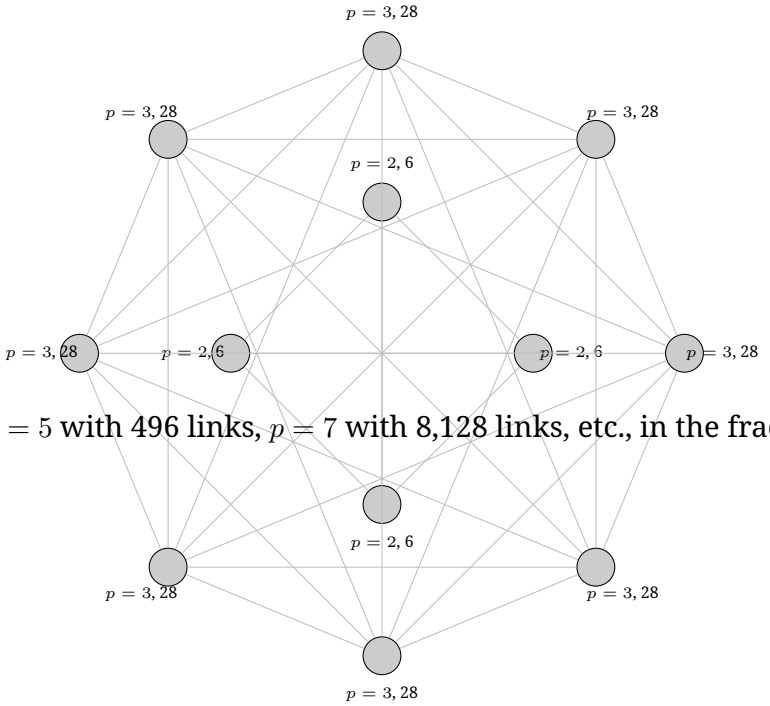
1 Diagram: Binary Fractal Lattice Closure for Perfect Numbers

This diagram illustrates the Allen Fractal Closure Law (AFCL) within Pattern Field Theory™ (PFT™), where even perfect numbers are binary fractal closure counts in the π-particle lattice. For prime p with 2^p-1 a Mersenne prime, $\text{Perfect}(p) = \binom{2^p}{2} = 2^{p-1}(2^p-1)$ represents the total pairwise links among 2^p nodes (diamonds in Differentiat™ geometry) arranged on nested rings, reflecting the fractal resonance of the Pi Matrix™ substrate.



(Scales to $p = 5$ with 496 links, $p = 7$ with 8,128 links, etc., in the fractal series)

Figure 1: Binary fractal lattice closure for perfect numbers $p = 2$ (6 links) and $p = 3$ (28 links), with nested rings representing the π-particle lattice in PFT™. Each ring's total pairwise links (light gray lines) equal the perfect number, illustrating the fractal resonance and structural invariance of the Pi Matrix™ substrate. Larger p values extend this pattern, aligning with physical and biological scales (e.g., 496 in superstring theory, 28-day cycles).